Probe-Configuration-Dependent Decoherence in an Aharonov–Bohm Ring

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(Received May 27, 2002)

We have measured transport through mesoscopic Aharonov–Bohm (AB) rings with two different four-terminal configurations. While the amplitude and the phase of the AB oscillations are explained well within the framework of the Landauer–Büttiker formalism, it is found that the probe configuration strongly affects the coherence time of the electrons, i.e., the decoherence is strongly reduced in the configuration of so-called nonlocal resistance. This result should provide an important clue in clarifying the mechanism of quantum decoherence in solids.

KEYWORDS: Aharonov–Bohm ring, phase coherence, nonlocal resistance, Landauer–Büttiker formula
DOI: 10.1143/JPSJ.71.2094

In mesoscopic physics, it is well known that probes for transport measurements greatly affect the electronic states of the samples. Particularly in single-electron phenomena, a low-impedance probe introduces coupling of the system to an electromagnetic environment and causes the degradation or even disappearance of the single-electron charging effect.1) In coherent transport, where probes and samples are strongly coupled, it was also recognized in early studies that “sample” and “leads” are difficult to distinguish.2)

In the coherent regime, however, unlike the case of single-electron phenomena, the quantum coherence of electrons has been believed to be independent of the probe configuration, that is, the selection of the pairs of voltage and current probes in a four-terminal measurement. This assumption is likely to be true for the diffusive transport regime because the electrons experience many elastic scatterings in traversing the sample from one probe to another, which would function as buffers to the environment. Actually, it has been verified both theoretically and experimentally that the phase coherence time (τφ) in this regime is the same regardless of the probe configurations.3) On the other hand, in ballistic transport, electrons pass into samples directly from the terminals, suggesting the possibility that the saturation is due to some extrinsic effects.

In this work we show that in the ballistic regime the coherence of electrons greatly depends on the probe configuration, through a four-terminal measurement of the same sample with two different probe configurations. First, we show that the Landauer–Büttiker (LB) formalism, which was constructed for coherent transport with all the probes treated equally,4) successfully describes the qualitative features of the present experiment. Next, this analysis is shown to lead to the inevitable conclusion that the decoherence is dependent on the probe configuration.

Fig. 1. (a) Scanning electron micrograph of the AB ring. One specific Au/Ti metallic gate marked “G” was used in this study. (b) Local four-terminal setup (current: 1 → 4, voltage: 2 → 3). (c) Nonlocal four-terminal setup (current: 1 → 2, voltage: 4 → 3).
pair at the opposite end is measured ($R_{12,43}$ and “nonlocal” setup).

In order to minimize the difference due to the instrumental effect, the same setup and parameters were adopted for both configurations except the current amplitudes, which were 3 nA and 15 nA for the local and nonlocal setups, respectively. It was confirmed that these currents do not cause a Joule heating effect. The resistances were measured by the standard lock-in technique. A cryogenic low-pass filter was inserted into every lead at the 1K stage. Two samples (#1 and #2) with almost the same geometry were measured, yielding essentially the same results.

The curves shown in the upper parts of Figs. 2(a) and 2(b) are the raw magnetoresistance traces for the local and nonlocal setups, respectively. The AB resistance oscillations with a period $\Delta R_{AB} = 3.1 \pm 0.5$ mT, consistent with the ring size, are superposed over the slower aperiodic fluctuation which arises from small conductance loops within branches. The lower parts of Figs. 2(a) and 2(b) present the AB component ($\Delta R_{AB}$) extracted through fast Fourier transform (FFT). In the local setup, $\Delta R_{AB}$ is only approximately 2% of the total resistance, which is a typical value for the oscillation amplitude seen in many previous AB experiments. In contrast, in the nonlocal setup, it averages up to 20% with a maximum of $\sim 75\%$. This is the largest AB amplitude ever reported.

We also performed electrostatic control of the electronic phase through the voltage of gate $G$ ($V_G$). The gray-scale plots in Fig. 3 show the gate-voltage-induced variation of the AB oscillation at 30 mK. The variation of the electrostatic potential energy by $V_G$ influences the kinetic energy, and hence the wave number of the electrons which traverse the region underneath the gate electrode.

Now we demonstrate that the qualitative features of the above results at the lowest temperatures are well explained within the LB framework. The LB formula gives

$$R_{mn,kl} = \frac{h}{2e^2} T_{mn} T_{lm} / D,$$

where $T_{ij}$ ($i \neq j$) is the transmission coefficient from terminal $j$ to $i$ and the denominator $D$ is a quantity including all of the $T_{ij}$'s. Here, we note that this formula, which was originally applied to perfect coherent transport, can be generalized to include incoherent transport. The generalized LB formula is expressed by the transmission coefficients that are the sum of a coherent part and an incoherent part, and has the same functional form as the original one. Thus the effect of decoherence is appropriately taken into account through the amplitude of the interference term in the transmission coefficients in the LB formula.

From the sample geometry shown in Fig. 1(a), we can readily approximate that $T_{12} = T_{21} = T_{34} = T_{43} \equiv T_0, T_{14} = T_{41} = T_{23} = T_{32} \equiv T_1$ and $T_{13} = T_{31} = T_{24} = T_{42} \equiv T_2$. In order to take the decoherence into account, transmission coefficients used for those paths traversing the ring ($T_1$ and $T_2$ in the present case) are taken as $T_{ij} = x_{ij} + y_{ij} \cos(2\pi \phi_0 + \delta_{ij})$, where $x_{ij}$ represents the AB amplitude, $y_{ij}$ the other part of the transmission, $\phi$ the magnetic flux which threads through the ring, and $\phi_0 \equiv h/e$ the flux quantum. $\delta_{ij}$ is the phase due to the difference between the paths. Although $x_{ij}$ also depends on the magnetic field and contains the terms due to the interference, $|y_{ij}/x_{ij}|$ serves as a good measure of the coherence of traversing electrons, where the bars denote the average over a certain range of magnetic field.

In the above approximation, the LB formula gives the resistances

$$R_{14,23} = \frac{h}{2e^2} (T_0 + T_1) (T_1 + T_2) \sim \frac{h}{4e^2} T_1 + T_2$$

$$R_{12,43} = \frac{h}{2e^2} (T_0 + T_1) (T_0 + T_2) \sim \frac{h}{4e^2} T_0^2,$$

where we further approximate that $T_0 \gg T_1, T_2$. Note that the information on the phase of the AB oscillation has been neglected in this approximation because of the symmetric assumption $T_{ij} = T_{ji}$. Equation (1) indicates that the ratio of the AB oscillation in $R_{14,23}$ directly reflects $\bar{\phi}/\bar{\pi}$, while in eq.

![Fig. 2](image_url) (a) The upper curve is a typical trace of $R_{14,23}$ in the local setup. The lower curve shows the AB component $\Delta R_{AB}$ extracted from $R_{14,23}$ through FFT filtering. (b) Corresponding data for the nonlocal setup.

![Fig. 3](image_url) Gray-scale plots of the AB oscillation components of the resistances as a function of $V_G$ observed in (a) the local setup and (b) the nonlocal setup.
the incoherent parts in $T_1$ and $T_2$ cancel each other by subtraction and the AB amplitude is emphasized in the magnetoresistance. This is the qualitative explanation for the results shown in Fig. 2.

Next, the phase modulation by the gate voltage $V_G$ in Fig. 3 is explained as follows. The applied gate voltage modulates the potential of electrons and hence their wave numbers, which results in the variation of $\delta_j$. According to a capacitance model between the gate and the 2DEG, the equi-phase curve of the AB oscillation in the B-$V_G$ plane should take the form $B = \Delta B_{ij} W k_B / 2 \pi (1 - |V_G/V_C|^2)^{1/2} + N$ ($N = 0, \pm 1, \ldots$), where $V_C$ is the pinch-off voltage ($-0.435$ V for the present case). This curve satisfactorily explains the overall trend of the phase shift in the nonlocal case as indicated by the white dashed lines in Fig. 3(b) (the curves for $N = -1, 0, 1$ are plotted). The phase jumps observed in a few regions are due to the intermixing effect of the conduction channels.

On the other hand, the phase variation in the local case differs greatly from that described above. It was established by early studies that in the LB framework the two-terminal resistance $R_{0}$ must be an even function of the magnetic field, i.e., $R_{0}(B) = R_{0}(-B)$, due to Onsager’s reciprocal theorem $T_{ij}(B) = T_{ji}(-B)$ and current conservation. The reciprocal theorem appears in four terminal resistances as $R_{ij,\text{me}(B)} = R_{ij,\text{me}}(-B)$, and $R_{ij,\text{me}}$ itself is not necessarily even with $B$. Hence, it is natural that the phase varies continuously with $V_G$ in the nonlocal setup. Actually, we experimentally confirmed that $R_{12,43}(B) = R_{13,12}(-B)$ holds. In the local setup, the current and voltage probes are placed crossing the ring part, which brings the situation close to the nonlocal case as indicated by the white dashed lines in Fig. 3(b) (the curves for $N = -1, 0, 1$ are plotted). The phase jumps observed in a few regions are due to the intermixing effect of the conduction channels.

Thus far, we have seen that the LB formula successfully describes the qualitative profiles of the results, which leads us to believe that the quantitative outcome of the formula can be used as a basis for the comparison between the two configurations. In order to estimate the classical $T_{ij}$’s, we measured the resistances for all of the possible probe configurations at 4.2 K where the quantum interference effect is small. By combining these values with the AB oscillation measured at various temperatures shown in Figs. 4(a) and 4(b), we obtain the temperature dependence of the portion of the interference term in the transmission coefficient $\delta T_{ij} / T_{ij}$ as shown in Fig. 4(c). A striking difference between the local and the nonlocal setup is observed: the ratio of the coherent term to the total transmittance is much higher in the nonlocal probe configuration and it is much more robust against thermal disturbance. As shown in Fig. 4(c), the consistency of results for the two different samples with the same geometry strongly indicates that this observation is not sample-specific but is due to the measurement configuration.

Two factors are important for the reduction of the AB amplitude with temperature. One is the thermal broadening of the electron wave packets, which is expressed in the ballistic case as $\beta_{ij} \propto \exp(-\tau_{i} k_{B} T / h) \equiv \exp(-\tau_{i} / \tau_{B})$, where $\tau_{B} = L / v_{F}$ ($v_{F}$: the Fermi velocity). The other is the quantum decoherence, which contributes as $\beta_{ij} \propto \exp(-aT)$, implying that $\tau_{B}$ is negligible or is also proportional to $T^{-1}$. The obtained values of $a$ are 0.72 and 1.0 K$^{-1}$ for the nonlocal results, while they are $a = 2.3$ and 2.5 K$^{-1}$ for the local ones. The thermal broadening has the effect $\exp(-\tau_{i} / \tau_{B}) \equiv \exp(-bT)$ with $b \sim 1$ K$^{-1}$ in the present case, which would be sufficient to explain the temperature dependence of the nonlocal result. Since the thermal broadening is an intrinsic effect, we attribute the observed probe-configuration-dependent effect to the difference in $\tau_{B}$.

Thus the next problem is to determine the origin of the difference in $\tau_{B}$ between the two setups, or rather the suppression of $\tau_{B}$ in the nonlocal setup. Here, we would like to note that the electric current flows differently in that electrons run quasi-ballistically between terminals 1 and 4 in the local setup, while no net current enters the interferometer in the nonlocal setup. In the LB method, zero net current is the consequence of the cancellation of back and forth currents through a sample, but these “currents” are merely means for the calculation and are not physical entities. What actually happens and what the LB formula actually describes is the observation is not sample-specific but is due to the measurement configuration.

We list here two candidates for the origin of this phenomenon. The first is that the electrons in the local setup suffer extra decoherence due to the charge fluctuation. It is proposed that in a ballistic AB ring the charge
fluctuations caused by a nearby capacitor such as metallic gates result in decoherence expressed as $\tau_0 \propto T^{-1}$, which is in agreement with our observation. A similar observation was reported by Hansen et al.\textsuperscript{12) In the local setup, charge fluctuation, which originates from shot noise\textsuperscript{13) due to the nonequilibrium current in the interferometer, may play a significant role when the net current exists. In the nonlocal setup, this mechanism is expected to be suppressed. The second mechanism is based on the deduction that in the local setup injected electrons traverse the ring quasi-ballistically and may retain some traces that can indicate “which path they went through” to the circumambient electrons in 2DEG.\textsuperscript{14) In other words, the interference does not complete at the outlet of the sample locally. This is expected to lead to a loss of coherence through the process discussed by Stern et al.\textsuperscript{15) In the nonlocal setup, the electrons in the ring are comparatively isolated from the leads by the electrostatic barrier formed by the charge up. This mechanism may be reduced by making the outlet narrower to prevent the leakage of the “which path” information.

In conclusion, we have observed that the quantum decoherence in a ballistic AB ring is dependent on the probe configuration. While $\tau_0$ behaves as $\propto T^{-1}$, in both local and nonlocal setups, the coherence survives at much higher temperatures in the nonlocal setup. We believe that the key difference is the amplitude of the net electric current, and plausible mechanisms are discussed. While theoretical effort is necessary to clarify this issue, the LB formula successfully describes the qualitative profiles of the results, such as the large amplitude of the AB oscillation in the nonlocal setup and the phase tuning by electrostatic potential.

**Acknowledgements**

We thank H. Ebisawa and H. Fukuyama for helpful discussions. This work is partly supported by a Grant-in-Aid for Scientific Research and by a Grant-in-Aid for COE Research (“Quantum Dot and Its Application”) from the Ministry of Education, Culture, Sports, Science, and Technology.